

**AN ARQ SCHEME USING FIXED-BOUNDARY SUBPACKETS  
WITH PILOT SYMBOL ASSISTED MODULATION  
FOR RAYLEIGH CHANNELS**

by

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B.A.Sc., University of Toronto, 2005

A PROJECT SUBMITTED IN PARTIAL FULFILLMENT  
OF THE REQUIREMENTS FOR THE DEGREE OF  
MASTER OF ENGINEERING

In the School  
of  
Engineering Science

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SIMON FRASER UNIVERSITY  
FALL 2006

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## ABSTRACT

A novel scheme of ARQ protocol using fixed-boundary subpackets to partition a packet for re-transmissions is presented. Monte Carlo simulations of transmitting PSAM signals using QPSK over Rayleigh channels with up to 3% Doppler have been used to evaluate the performance of the proposed technique. Benchmarking against an ARQ protocol using CRC for error detection, this subpacket ARQ scheme provides up to 35% and 7% better in throughput for packets that are longer than 1024 when the channel SNR is greater than 25dB without Doppler and with 1% Doppler respectively. Future extensions of this subpacket re-transmission scheme with PSAM may lead to higher throughput in other ARQ protocols currently using CRC for error detection.

**Keywords:** ARQ; error detection; subpacket scheme; PSAM; Rayleigh channel

**Subject Terms:** Data transmission systems; digital communications; mobile communications systems; wireless communication systems

## **ACKNOWLEDGEMENT**

I wish to express my gratitude to Professor Paul Ho of Simon Fraser University for providing me with the subject of this project, as well as his continuous encouragement and guidance throughout the course of this research. Furthermore, I must thank Professor James Cavers of Simon Fraser University for providing valuable feedback in strengthening the reliability of the proposed protocol. I would also like to acknowledge the generous support from TELUS Technology Strategy for providing the additional computing facilities required in the final stages of this research.

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## I. INTRODUCTION

Automatic Repeat reQuest (ARQ) protocol involves a receiver using a feedback mechanism to request the transmitter to re-send the packets detected as erroneous. Cyclic redundancy check (CRC) is typically used for detecting errors hence determining whether the received packets are the error-free version of the original message transmitted. File transfer protocol (FTP) and the Institute of Electrical and Electronics Engineers (IEEE) 802.11x Wireless Local Area Network (LAN) standards are two of the many applications using CRC in ARQ [1]. When the CRC does not check at the receiver, this information will either be explicitly or implicitly feedback from the receiver to the transmitter requesting a re-transmission of the erroneous message [2,3]. Existing ARQ protocols vary in the maximum number of repeat requests before dropping a packet for re-transmissions, the content of the packet during the re-transmissions, as well as the handling of the multiple packets received from the requested re-transmissions [4].

Conventional pure-ARQ uses an error detecting code and a feedback channel to initiate re-transmission of any packets received in error. Over the years, there have been numerous extensions in pure-ARQ protocol. Today, pure-ARQ remains attractive because including only error detection code has a lower overhead than using error correction coding. Nevertheless, pure-ARQ is generally combined with a moderate degree of error correction coding (Hybrid ARQ) in order to increase the system throughput by reducing the number of retransmissions required [5]. At a high level

overview, there are three types of Hybrid ARQ (HARQ). Type-I HARQ mostly combines pure-ARQ and forward error correction (FEC) coding; Type-II HARQ or Chase Combining (CC), is a solution of combining multiple copies of the same signals using maximal ratio combining (MRC); Type-III HARQ involves incremental redundancy (IR) whereby the additional coded parities are retransmitted [6,7]. 1X Evolution Data/Voice (1XEV-DV) and High-Speed Downlink Packet Access (HSDPA) are two of the many wireless communication standards that have adopted various forms of HARQ protocols [8].

Researches in various ARQ and HARQ schemes have been on-going over the past few decades. Some of the developments in the past few years include various rate-adaptive ARQ protocols [1], an HARQ scheme using product code comprised of two CRC codes [9], the determining of optimum packet size dynamically based on a given bit-error-rate (BER) [10], the use of arithmetic coding to control the amount of redundancy in re-transmission [2], employing adaptive modulation and coding (AMC) in HARQ [11], as well as leveraging cooperative relaying extension in ARQ [4].

Until recently, most of the work continues to optimize ARQ protocols by considering the re-transmission of the packet in its entirety. Extending the packet combining system using Viterbi Decoder by [12], [13] recently proposed an adaptive system in determining the optimum number of subpackets used in a convolutionally coded system with binary-phase-shift keying (BPSK) subjected to additive white Gaussian noise (AWGN).

In this project, a novel scheme for pure-ARQ in Rayleigh fading channels using fixed-boundary subpacket partitioning of a packet for re-transmissions to improve the

overall channel throughput is presented. Pilot symbol assisted modulation (PSAM) signals are transmitted using quaternary-phase-shift-keying (QPSK) and Rayleigh channels with fade rates up to 3% have been used to evaluate the performance of the proposed scheme. In the proposed technique, the magnitude of the received signals,  $|r|$ , and the magnitude of the compensated received signals,  $|g*r|$  are used as thresholds in determining the re-transmission requirement. The baseline of comparison is an ARQ protocol with CRC for error detection.

Section II discusses the system models of the baseline scheme and the proposed scheme. The first two subsections in section III present the Monte Carlo simulation results of the throughputs and the drop-rates for the baseline system as well as the proposed systems at different signal-to-noise ratios (SNRs) with different fade rates using various subpacket sizes. Section III.C compares the performance between the baseline and the proposed schemes. Section IV recommends the possible extensions based on the results presented and section V concludes the project.

## II. SYSTEM MODEL

This section is organized in the following manner. The general assumptions and considerations common to both the baseline and the proposed schemes will first be presented. Subsection II.B presents the CRC scheme used as the benchmark, and subsection II.C outlines the details of the proposed subpacket scheme.

### A. General Assumptions and Considerations

The assumptions and considerations made in this project are as follows:

- 1) The channel conditions in the feedback (uplink) direction (i.e., from the receiver to the transmitter), and the feed-forward (downlink) direction (i.e., from the transmitter to the receiver) are reciprocal.
- 2) The maximum total number of transmission is six times including the initial transmission (i.e., maximum of five re-transmissions).
- 3) A pilot spacing of seven and a filter length of eleven are chosen to be the parameters of the PSAM to accommodate normalized fade rates of up to 3% [14].
- 4) The size of the overhead contained in a packet for synchronization at the receiver is considered negligible.
- 5) The system uses quaternary phase-shift-keying (QPSK) constellations.
- 6) The Rayleigh channel SNRs studied are 15dB, 17dB, 19dB, 21dB, 23dB, and 25dB.
- 7) The normalized fade rates studied are 0, 1%, and 3%.

In this project, three packet sizes of 280, 560, and 1400 symbols are considered. Packet sizes are chosen to be multiples of 7 to facilitate the composition of the individual PSAM frames of length 7.

## B. Additional Considerations of the Baseline Scheme

In the baseline scheme, the receiver sends out an acknowledgement (ACK) when the CRC of a packet is successful at the receiver. In the case of a failed CRC, the entire packet will be re-transmitted from the transmitter to the receiver until either an ACK is achieved or the maximum number of transmissions has been reached. In this project, the CRC-16 Consultative Committee of International Telephone and Telegraph (CRC16-CCITT) standard was chosen as the benchmark scheme. Specifically, the generator polynomial is 0x1021 in hexadecimal notation or  $D^{16} + D^{12} + D^5 + 1$  [13].

Figure 1 shows the packet structure of the baseline scheme. The terms used in the diagram will be referenced when presenting the throughput analysis calculations in section III.B.

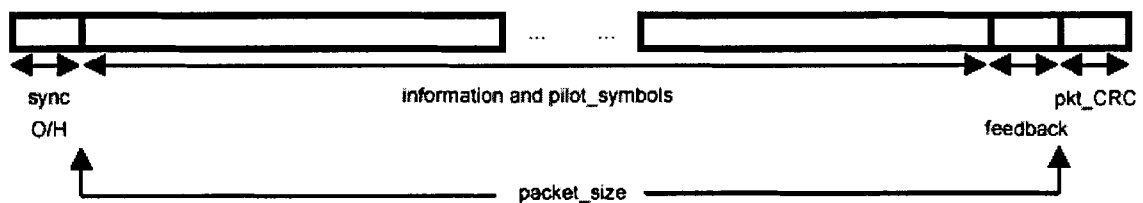


Figure 1. Packet structure of the baseline scheme

## C. Additional Considerations of the Proposed Scheme

Unlike the baseline scheme where the entire packet will be re-transmitted when it is not acknowledged before timer expiry, a frame of the proposed scheme may contain

subpackets belonging to one or more packets. The subpackets transmitted in each frame will be assembled at the receiver based on its subpacket and packet sequence numbers. The method of partitioning a packet into subpackets will be discussed later in this section. Figure 2 shows the frame structure of the subpacketing scheme and Table 1 explains the terms used in the diagram.

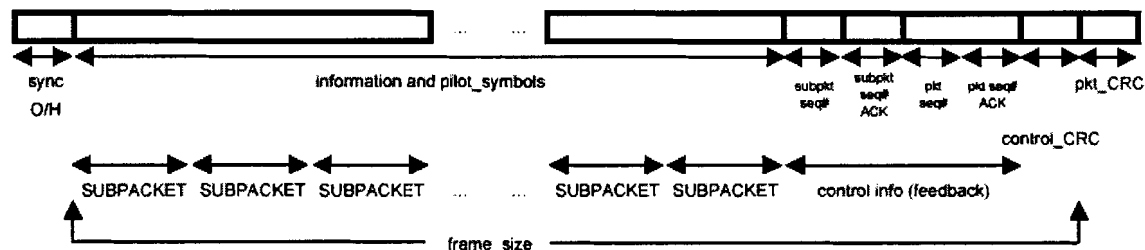


Figure 2. Frame structure of the proposed fixed-boundary subpacket scheme

Table 1. Definitions of terms used in Figure 3

control_CRC	CRC for the control_info
control_info (feedback)	A term for describing subpkt seq#, subpkt seq# ACK, pkt seq#, and pkt seq# ACK collectively
frame_size	A combinations of subpackets with information belonging to one or more packets
packet_size	A stream of symbols containing information belonging to a single packet
pkt seq#	Mod-8 (3 bits) sequence numbers indicating which packet does a subpacket belongs to. Mod-6 is chosen because the maximum number of re-transmission before dropping a subpacket is 5. Every subpacket has its own pkt seq#.
pkt seq# ACK	Mod-2 sequence numbers of the most recent correctly received packets
pkt_CRC	CRC for packet_size in the baseline scheme. For the proposed scheme, it is applied at the receiver to an assembled packet (i.e., a concatenation of subpackets belonging to the same packet)
subpkt seq#	Mod-2 sequence numbers of the subpackets

subpkt seq# ACK	Mod-2 sequence numbers of the most recent correctly received subpackets
sync O/H	Synchronization overhead

In the proposed scheme, PSAM is used to estimate channel state information (CSI) at the receiver. Leveraging the CSI, the receiver will check whether  $|r|$  and  $|g*r|$  from the received signals both exceed their respective threshold values set a priori at the receiver. For a symbol that failed to meet the thresholds, it will be re-transmitted as part of the subpackets that it belongs to. The rationale of using values of  $|r|$  and  $|g*r|$  as the error-detection thresholds at the subpacket level will be discussed later in this section. The interaction between using the threshold criteria in identifying subpackets requiring re-transmission, and having CRC at the receiver to detect errors for a packet (not a frame) will now be discussed. It is to note that for this proposed scheme, the use of CRC at the receiver scheme, in combination with using the CSI from PSAM, ensures that the error detection capability is the same as the baseline scheme.

When A sends messages to B, B checks the CRC of each assembled packet. At this time, one of three scenarios will occur prior to B feeding back any sequence numbers or acknowledgement (`control_info`) to A.

- 1) *If a packet CRC (`pkt_CRC`) is successful for an assembled packet at B:* B acknowledges the subpackets belonging to this packet by updating the corresponding ACK parts of the subpacket sequence numbers (`subpkt seq#`) and packet sequence numbers (`pkt seq#`). When the CRC of an assembled packet is successful, the subpackets belonging to this packet will not be flagged for re-



transmission even if these subpackets failed the threshold criteria. Other subpackets in the same frame belonging to other packets will be treated according to the outcome of their respective pkt\_CRC.

- 2) *If a packet CRC (pkt\_CRC) fails for an assembled packet at B and some of the subpackets belonging to this packet also failed the threshold criteria:* B acknowledges the subpackets belonging to this packet that passed the threshold criteria. For the subpackets belonging to this packet that failed the threshold criteria, B will receive a re-transmission after timer expiry at A. Other subpackets in the same frame belonging to other packets will be treated according to the outcome of their respective pkt\_CRC.
- 3) *If a packet CRC (pkt\_CRC) fails for an assembled packet at B and all of the subpackets belonging to this packet passed the threshold criteria:* B does not acknowledge the subpackets belonging to this packet that passed the threshold criteria. B will therefore receive a re-transmission of these subpackets after timer expiry at A. Other subpackets in the same frame belonging to other packets will be treated according to the outcome of their respective pkt\_CRC. This scenario should be a rare case.

When A receives the control\_info from B, one of two scenarios will occur depending on the received control\_CRC at A.

- 1) *If the control CRC (control\_CRC) fails at A:* A re-sends the entire frame sent to B in the previous time-slot.

2) *If the control CRC (control\_CRC) passes at A:* For the subpackets with acknowledged subpacket sequence numbers (i.e., subpkt seq# equals to subpkt seq# ACK), new subpackets get slotted into these positions. For the subpackets without acknowledged subpacket sequence numbers (i.e., subpkt seq# does not equal to subpkt seq# ACK), the same subpackets will be re-transmitted in these positions.

In choosing the parameters to be used for the threshold criteria, three separate scenarios using only one parameter (i.e., using only  $|r|$  for one case, only  $|g^*r|$  for another case, and only  $|g^*r|$  for the third case) were initially considered. The conclusion was that using one parameter for error flagging will quickly require all the symbols to be re-transmitted consequently decreasing the throughput of the system significantly. Therefore, this subpacket scheme uses both values of  $|r|$  and  $|g^*r|$  as the error-detection thresholds instead of using only  $|r|$  or  $|g^*r|$ . The  $|r|$  and  $|g^*r|$  threshold values are determined empirically through the Monte Carlo simulations prior to the numerical investigation of throughput and drop-rates.

In addition to the assumptions and considerations already covered, the proposed scheme divides the packet into smaller subpackets by using fix boundaries. For instance, a packet length of 280 with subpacket size of 5 results in 56 subpackets for the packet. Specifically, the second subpacket consists of the 6<sup>th</sup> to the 10<sup>th</sup> symbols of the packet. Should any symbols in this second subpacket failed to surpass the two threshold criteria, the 6<sup>th</sup> to the 10<sup>th</sup> symbols grouped as the second subpacket will be re-transmitted. In other words, one acknowledgement (subpkt seq# ACK) is used for acknowledging one or

multiple erroneous symbols within the same fixed-boundary subpacket before timer expiry. Contrasting to the use of dynamic boundaries where one possible implementation is to always transmit two adjacent symbols on both sides of a flagged symbol, the choice of using fixed-boundary subpackets, reduces the overhead required in providing sequence numbers and the respective acknowledgement. Using fix boundaries therefore eliminates another layer of complexity in this proof-of-concept investigation. In the proposed scheme, the subpacket sizes with fixed-boundary are 4, 5, 7, 10, 14, 28, 70, and 140. With the three packet sizes studied, the number of subpackets depends on the subpacket and packet sizes under consideration. Table 2 summarizes the settings considered in this project.

Table 2. Number of fixed-boundary subpackets for different packet and subpacket sizes

Number of Subpackets		Subpacket Size							
		4	5	7	10	14	28	70	140
Packet Size	280	70	56	40	28	20	10	4	2
	560	140	112	80	56	40	20	8	4
	1400	350	280	200	140	100	50	20	10

Moreover, the number of control symbols (i.e., control\_info), containing information on sequence numbers and acknowledgements, to be taken into account when calculating the channel throughput is dependent on the packet and subpacket size studied. For each subpacket, 1 bit is allocated for subpkt seq#, subpkt seq# ACK, and pkt seq# ACK; 3 bits are allocated for pkt seq#. With 2 bits in each QPSK symbol, every subpacket is associated with three symbols of control information. In order words, for each scenario considered in Table 2, the identification overhead associated is three times

the number of subpackets in the setting under consideration. Table 3 outlines the number of symbols required to relay re-transmission information to the transmitter.

Table 3. Identification overhead based on different frame and subpacket sizes

Number of Symbols for control_info		Subpacket Size							
		4	5	7	10	14	28	70	140
Frame Size	280	210	168	120	84	60	30	12	6
	560	420	336	240	168	120	60	24	12
	1400	1050	840	600	420	300	150	60	30

### III. SIMULATION RESULTS

The Monte Carlo simulations of this project are implemented using MatLab. Subsection A discusses the results of setting the thresholds. Subsections B and C analyze the throughput and drop-rate respectively. Subsection D discusses the overall system performance. As discussed in the previous section, the error detection reliability of the proposed scheme is the same as using CRC. Consequently, a subsection analyzing the undetected error probabilities is not required to warrant the overall system performance.

#### A. Threshold Settings

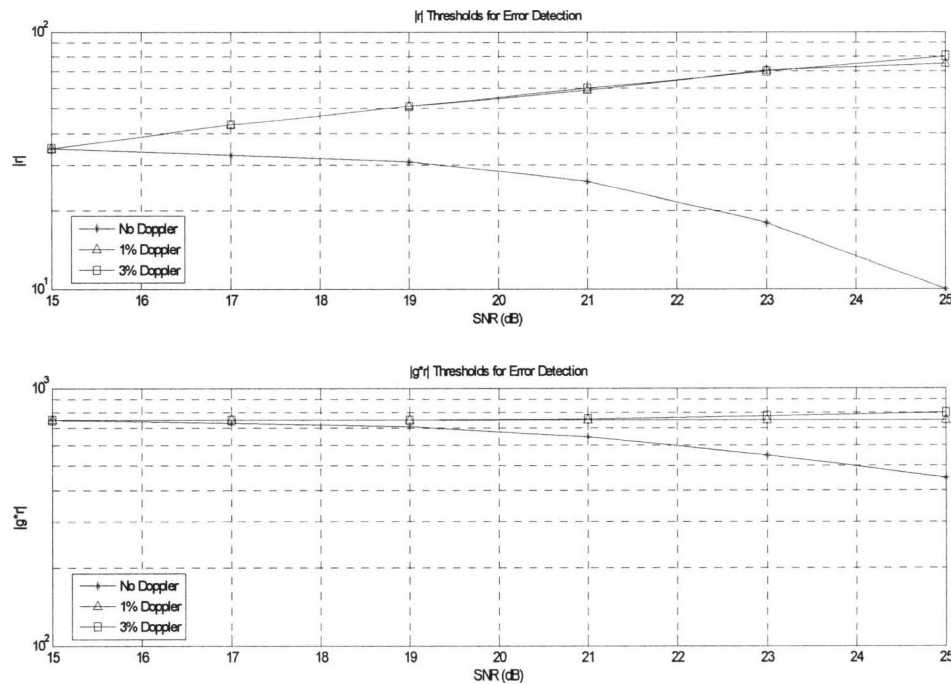


Figure 3. Thresholds of  $|r|$  and  $|g*r|$  for error detection

Figure 3 presents the absolute threshold values (i.e., not normalized values) used for this project. In scenarios where Doppler does not exist, the thresholds for  $|r|$  have an inverse relationship with the channel SNR. Contrasting to the no Doppler scenarios, the thresholds for  $|r|$  in the 1% and 3% Doppler scenarios have a direct relationship with the channel SNR. The higher thresholds in the presence of Doppler can be explained due to filter mismatch.

On the other hand, the thresholds for  $|g^*r|$  appear to be less sensitive to the channel SNR. This is expected because the values of  $|g^*r|$  in PSAM have already accounted for the CSI, including the channel SNR, implicitly. The thresholds of  $|g^*r|$  serve as a joint error detection criterion to reduce the number of false alarms. In this project, the thresholds of  $|g^*r|$  and  $|r|$  are determined empirically. Consequently, one possible extension to this work is to threshold the magnitude of the real and imaginary parts of the maximum-likelihood decision variables at the receiver analytically using techniques discussed in [15].

## **B. Throughput Analysis**

From the results of the Monte Carlo simulations, the average number of transmissions per packet for the CRC scheme, or per subpacket for the proposed scheme, is obtained for a given channel SNR and a normalized fade rate. The average number of transmissions for a packet using the baseline scheme is represented by  $\overline{N_{CRC}}$ ; the same quantity using the proposed subpacket scheme is represented by  $\overline{N_{subpkt=x}}$ . A drop-rate is also calculated for the packets that were not successfully transmitted after five re-transmissions and those results are presented in the next subsection.

In the baseline scheme, using the notations introduced in Figure 1, the throughput,  $\eta_{CRC}$ , is calculated by:

$$\eta_{CRC} \cong \frac{(packet\_size - pilot\_symbols - feedback)}{N_{CRC} \times (packet\_size + pkt\_CRC)}.$$

In the proposed scheme, using the notations introduced in Figure 2, the throughput,  $\eta_{subpkt=x}$ , is calculated by:

$$\eta_{subpkt=x} \cong \frac{(frame\_size - pilot\_symbols - control\_info - control\_CRC)}{N_{subpkt=x} \times (frame\_size)}.$$

Figures 4 to 9 capture the throughput results obtained from the simulations. In the legends of the plots, “Subpkt Size: x” and “CRC-16 Baseline” denote the proposed scheme with a subpacket size of x and the benchmark CRC16-CCITT scheme respectively.

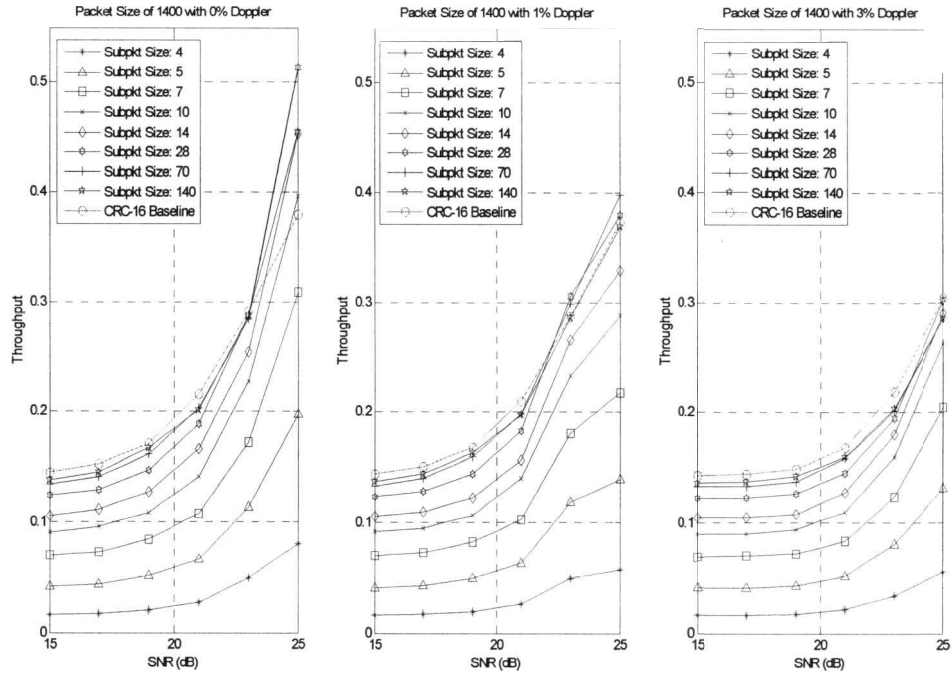


Figure 4. Throughput for packet length of 1400: 15dB to 25dB channel SNR

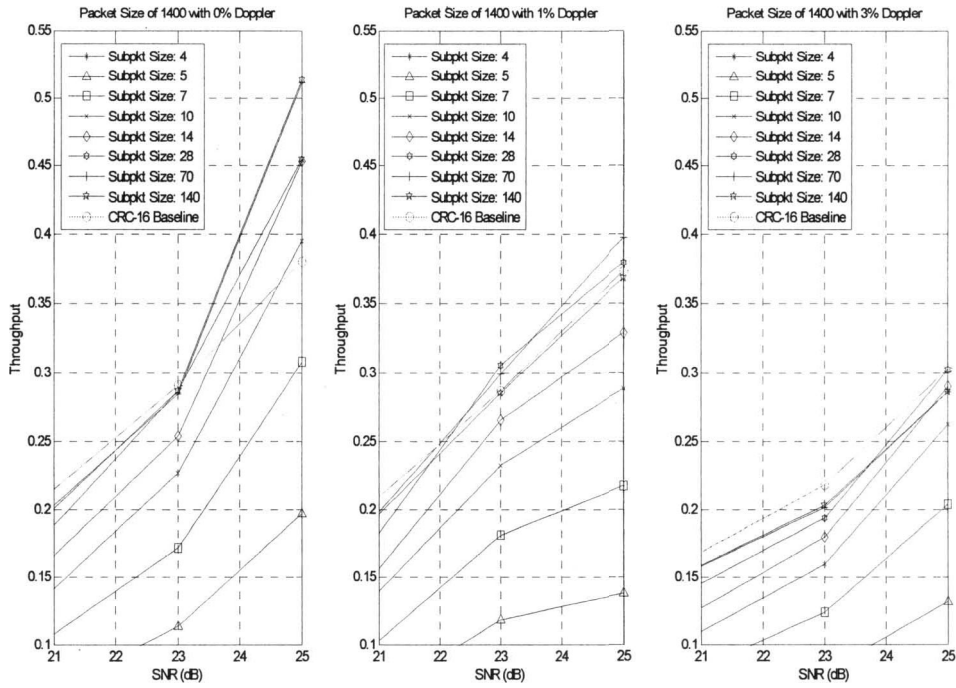


Figure 5. Throughput for packet length of 1400: 21dB to 25dB channel SNR



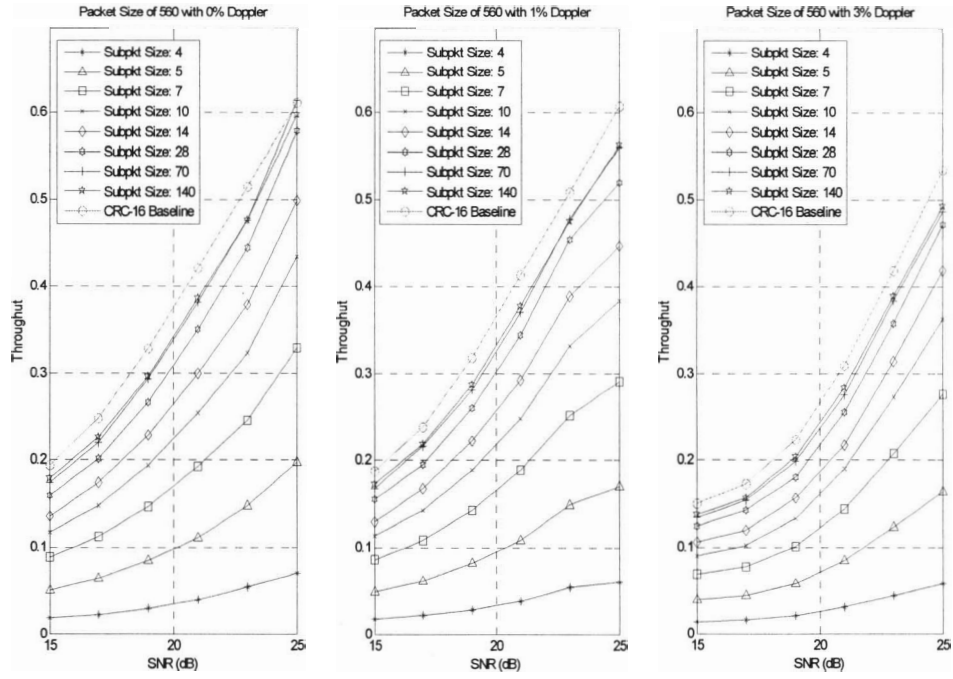


Figure 6. Throughput for packet length of 560: 15dB to 25dB channel SNR

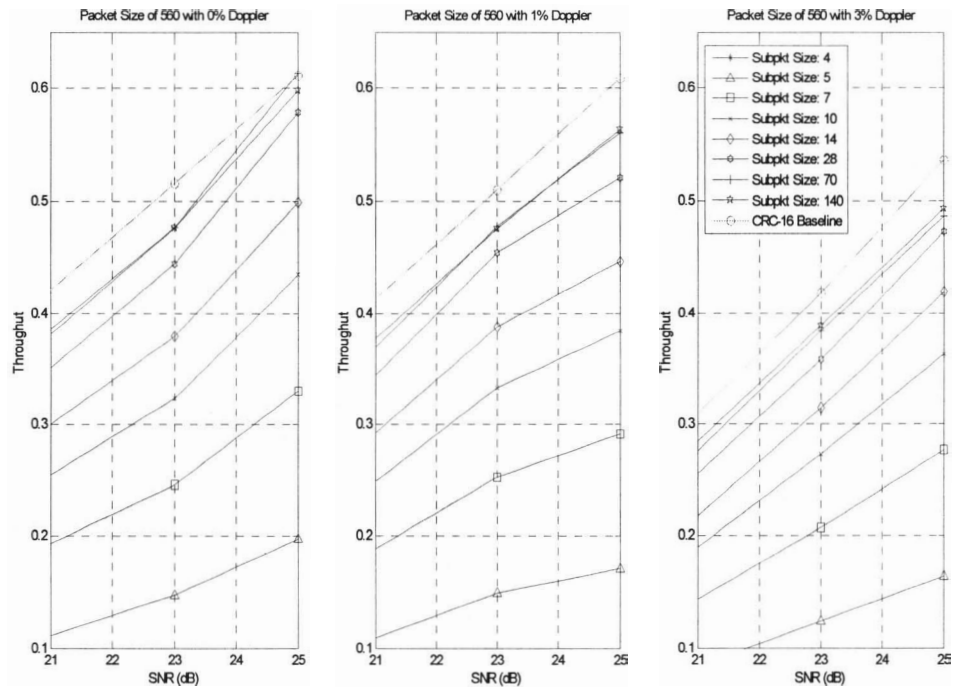


Figure 7. Throughput for packet length of 560: 21dB to 25dB channel SNR

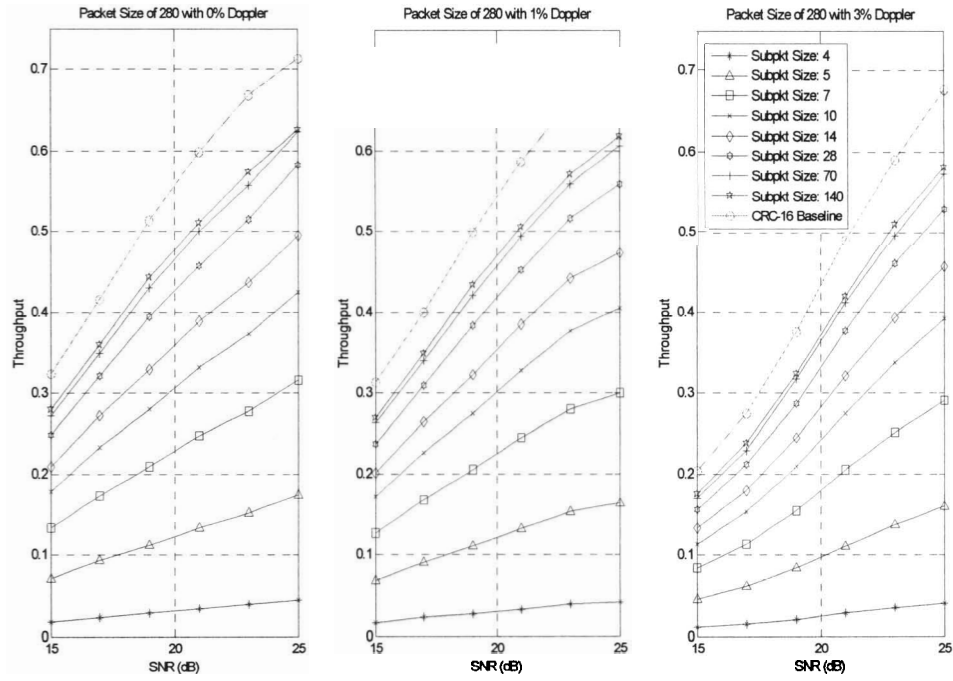


Figure 8. Throughput for packet length of 280: 15dB to 25dB channel SNR

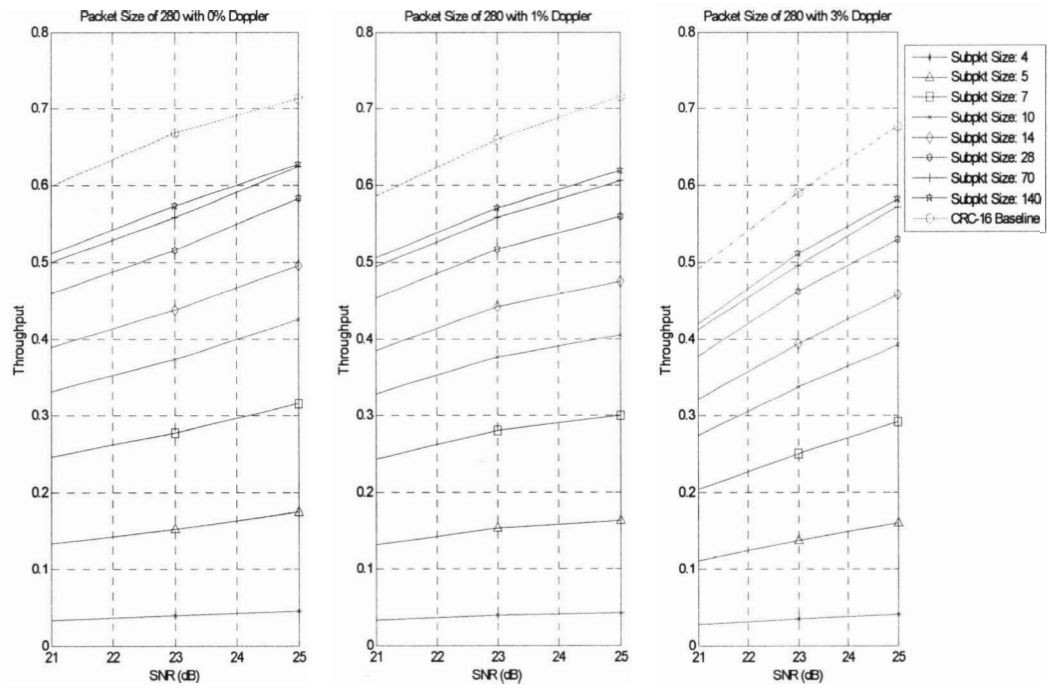


Figure 9. Throughput for packet length of 280: 21dB to 25dB channel SNR

The results to be noted are that at 25dB SNR, there exist solutions for the fixed-boundary subpacket sizes to have a comparable or higher throughput than that of the baseline CRC case. Moreover, Figures 4 and 5 show that for a packet length of 1400, there exists subpacket sizes of which a throughput higher than the baseline can be achieved at a SNR of 25dB. The implications of these results will be examined at a closer look in subsection D after the presentation of the drop-rate in the next subsection.

### **C. Drop-Rate Analysis**

The drop-rate is the quotient for the number of dropped packets divided by the number of packets attempted for transmissions. Understanding the drop-rate of the proposed scheme is important because a novel technique with only a higher throughput will be a less attractive alternative than one with both better throughputs and lower drop-rates. Figures 10 to 15 capture the drop-rate results obtained from the simulations. Similar to Figures 4 to 9, “Subpkt Size: x” and “CRC-16 Baseline” in the legends denote the proposed scheme with a subpacket size of x and the benchmark CRC16-CCITT scheme respectively.

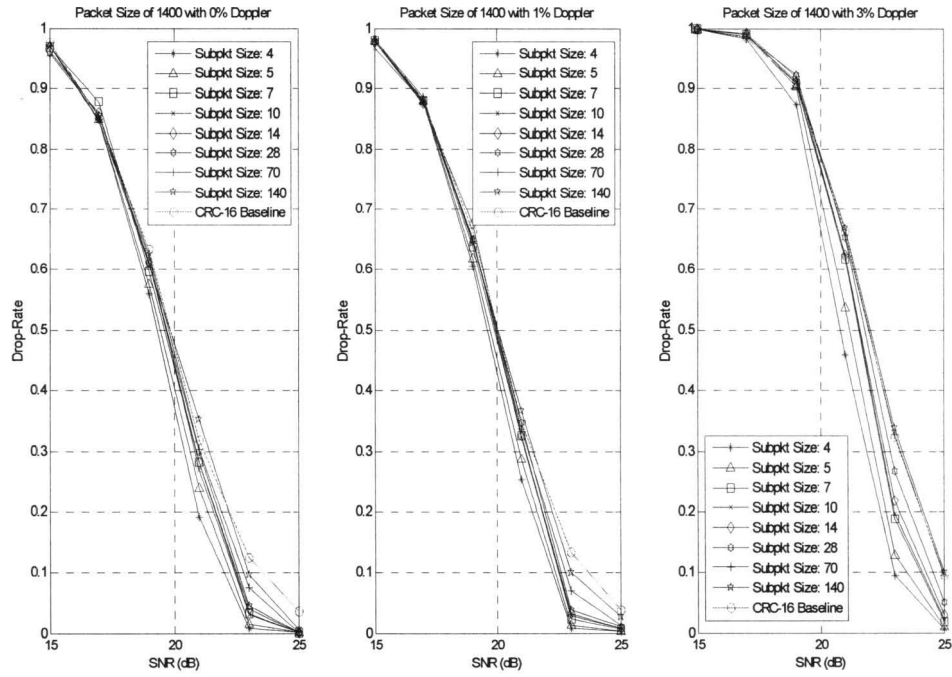


Figure 10. Drop-rate for packet length of 1400: 15dB to 25dB channel SNR

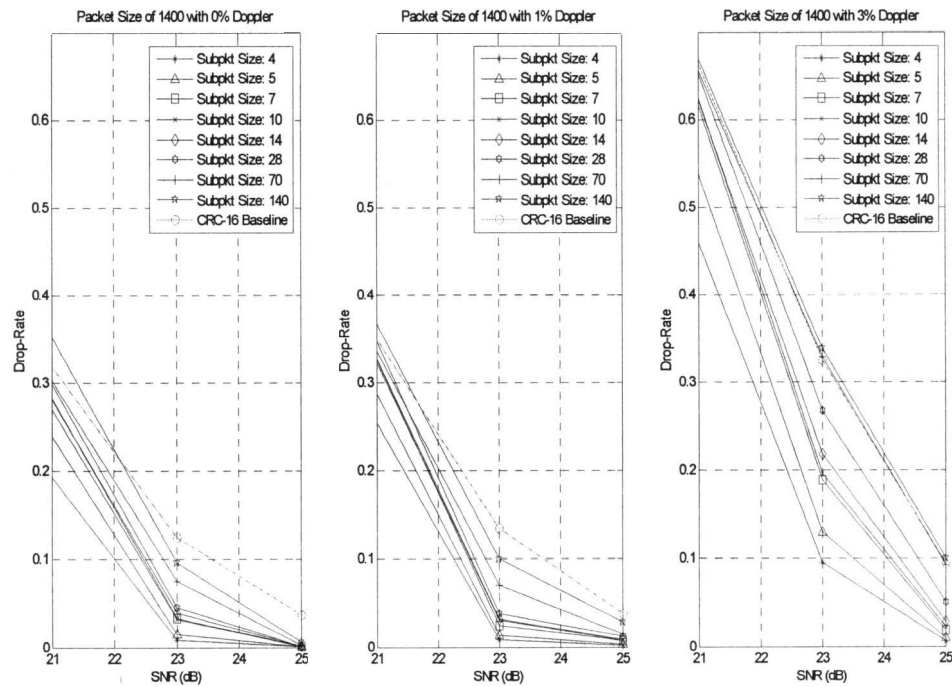


Figure 11. Drop-rate for packet length of 1400: 21dB to 25dB channel SNR

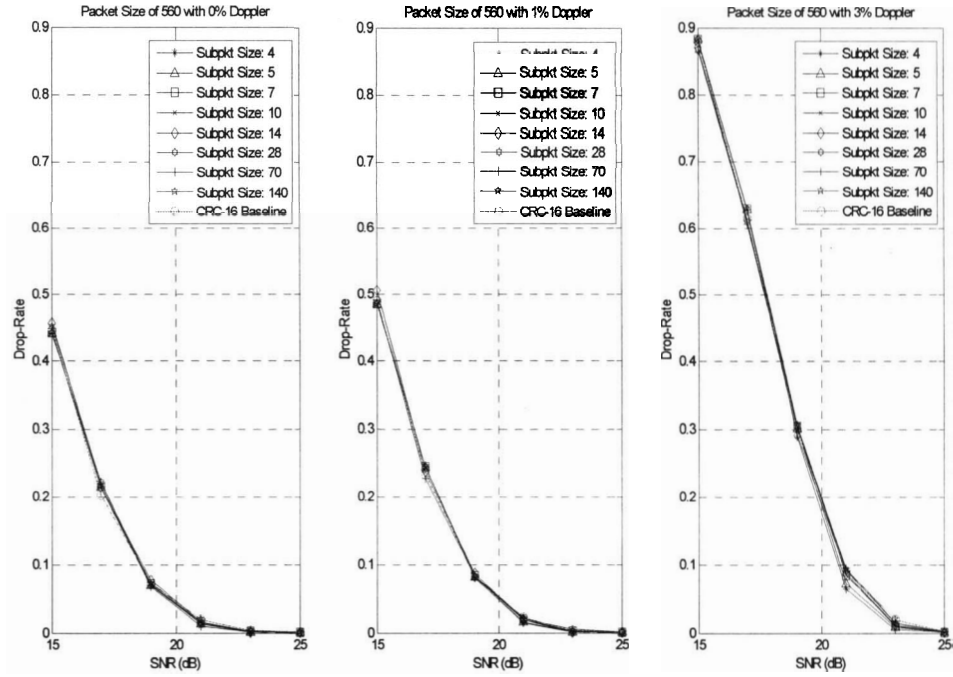


Figure 12. Drop-rate for packet length of 560: 15dB to 25dB channel SNR

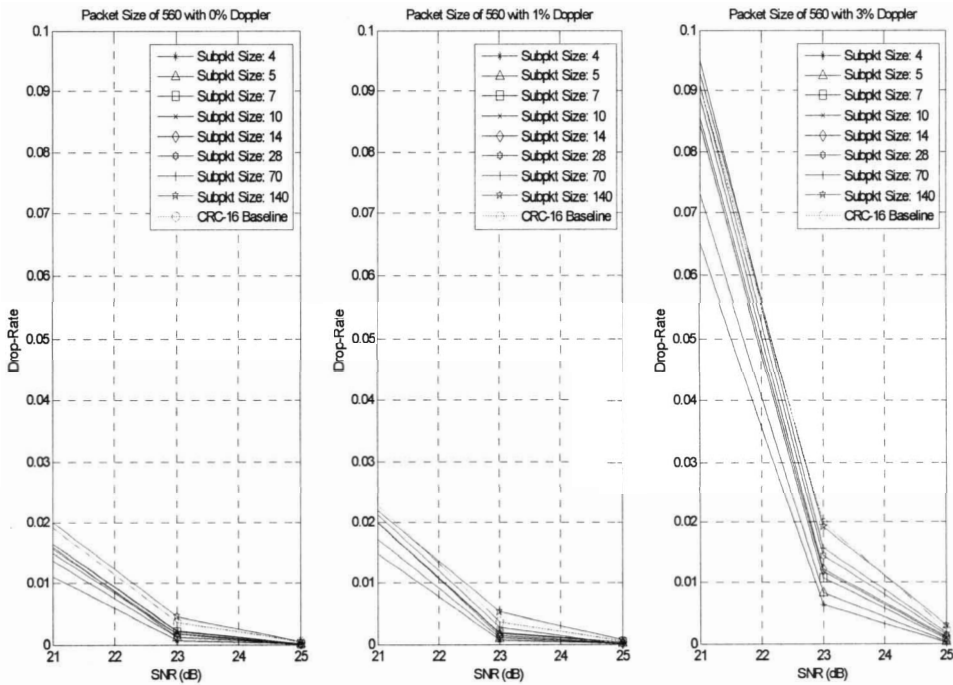


Figure 13. Drop-rate for packet length of 560: 21dB to 25dB channel SNR

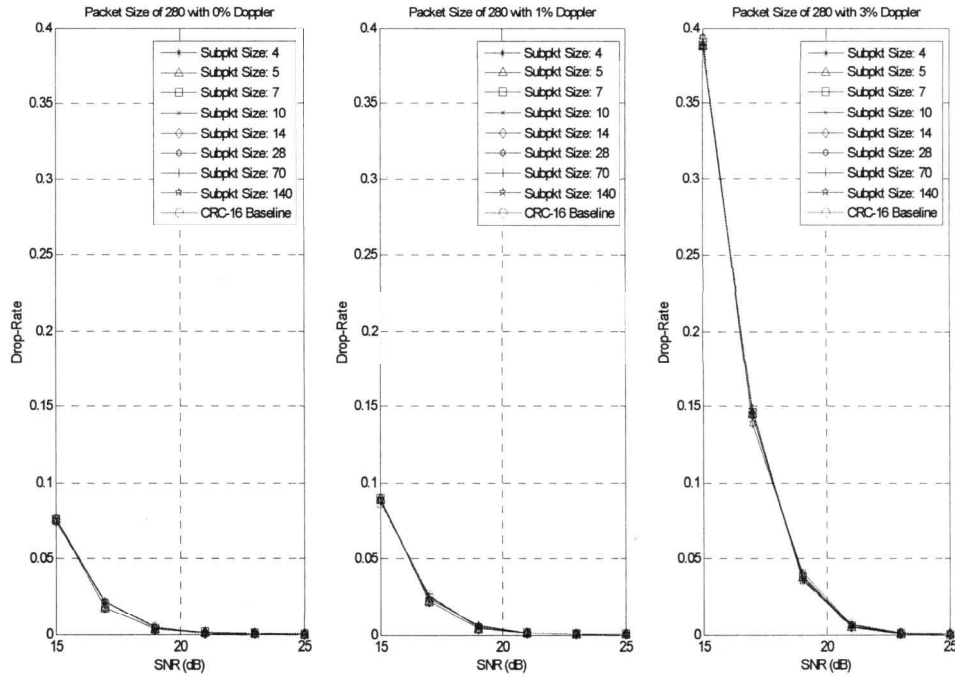


Figure 14. Drop-rate for packet length of 280: 15dB to 25dB channel SNR

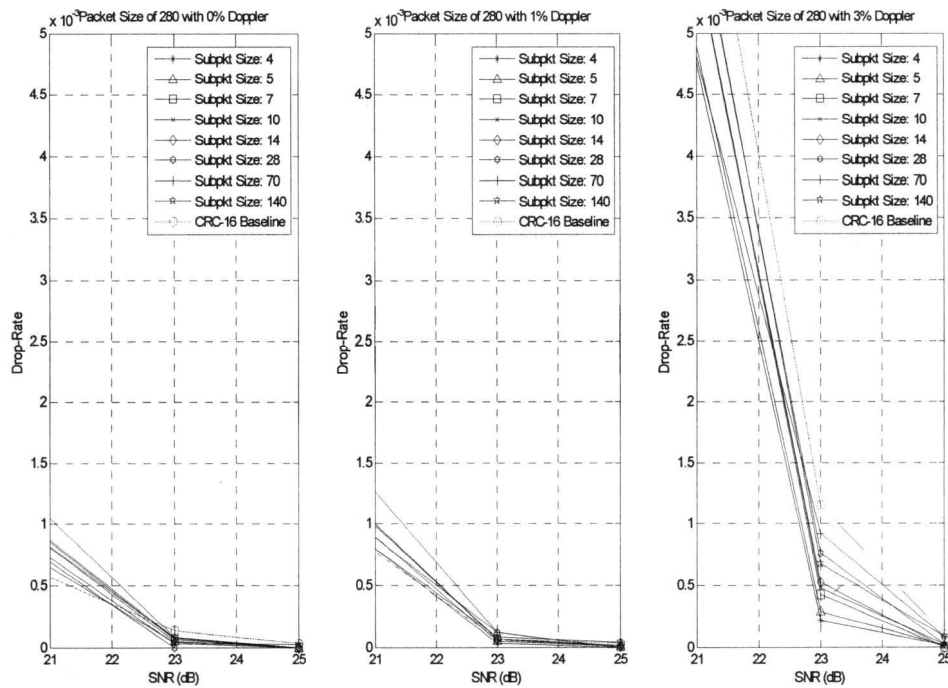


Figure 15. Drop-rate for packet length of 280: 21dB to 25dB channel SNR

The results to be noted are that at 25dB SNR, there exist solutions for the fixed-boundary subpacket sizes to have a comparable or lower drop-rate than that of the baseline CRC case. The implications of these results in combination with the throughput results will be examined in the next subsection.

## **D. Overall System Performance Analysis**

In assessing the overall ARQ protocol performance of two schemes, the error detection capability, the throughput and the drop-rate are crucial metrics. Because the error detection capability for the proposed scheme is the same as the baseline scheme, only a higher throughput and a lower drop-rate together may qualify this proposed ARQ scheme to be an attractive proposition.

### **1) Throughput Comparison**

Figures 16 to 18 show that the proposed scheme either has the same or a better throughput at SNR of 25dB for some subpacket sizes studied.

Expressed in percentage, a positive throughput gain is the throughput improvement that the proposed scheme has over the baseline scheme. For instance, if the proposed scheme has a throughput of 75% while the baseline scheme is at 60%, the throughput gain reported will be 25%. Based on the throughput gain in the proposed scheme from the baseline as shown in Figure 16, Table 4 shows the results for a packet size of 1400, at 25dB channel SNR with the fade rates studied

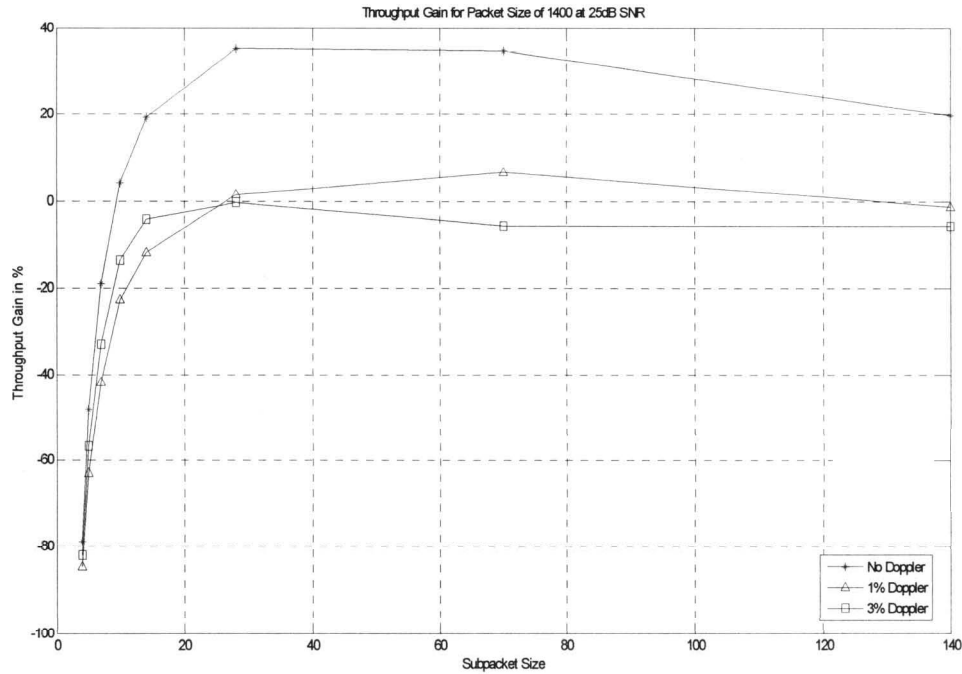


Figure 16. Throughput gain for packet length of 1400 at 25dB

Table 4. Throughput gain for packet length of 1400 at 25dB with 0%, 1% and 3% Doppler

Throughput Gain in %		Subpacket Size of 1400 at 25dB SNR							
		4	5	7	10	14	28	70	140
Fade Rate	0%	-78.91	-48.17	-18.89	4.17	19.35	35.16	34.61	19.79
	1%	-84.82	-62.97	-41.80	-22.66	-11.84	1.64	6.73	-1.22
	3%	-81.97	-56.81	-32.95	-13.47	-4.25	-0.27	-5.70	-5.65

In Table 4, the simulation results indicate that at 25dB without Doppler, using subpacket sizes of 28 and 70 for a packet length of 1400 leads to a throughput gain of 35%. Moreover, at a moderate Doppler of 1%, there remains over 6.5% in throughput gain when subpacket size of 70 is employed.



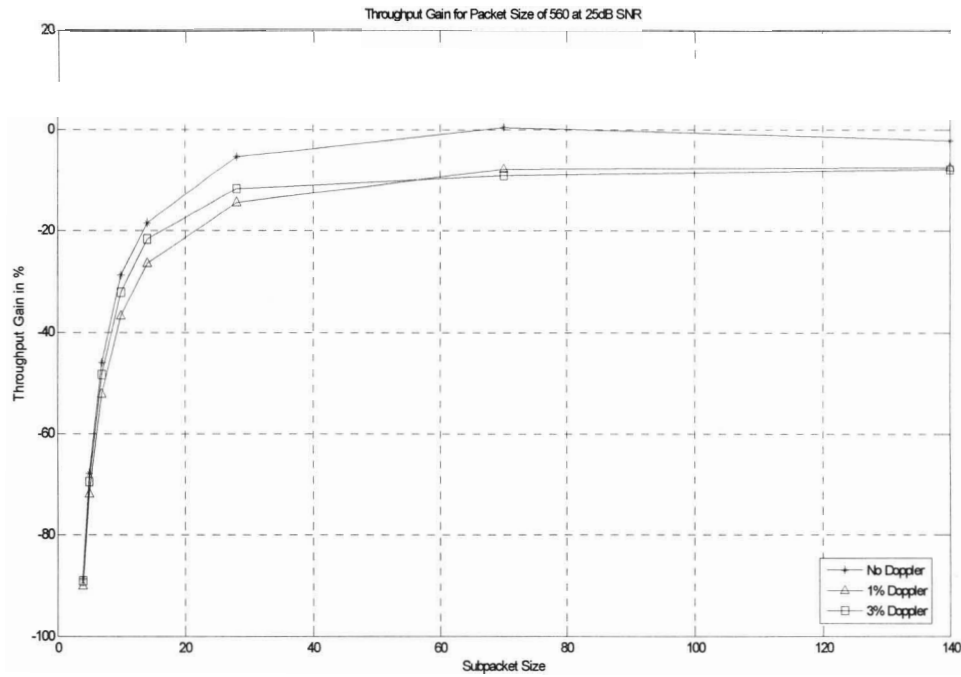


Figure 17. Throughput gain for packet length of 560 at 25dB

Table 5 shows the throughput gain for a packet size of 560, at 25dB channel SNR without Doppler from Figure 17. Using a subpacket size of 70 for a packet size of 560 achieves the best throughput result. The result, however, is only slightly better than the baseline scheme with a 0.3% gain.

Table 5. Throughput gain for packet length of 560 at 25dB without Doppler

Throughput Gain in %	Subpacket Size of 560 at 25dB SNR							
	4	5	7	10	14	28	70	140
Fade Rate 0%	-88.64	-67.79	-46.03	-28.94	-18.42	-5.39	0.30	-2.21

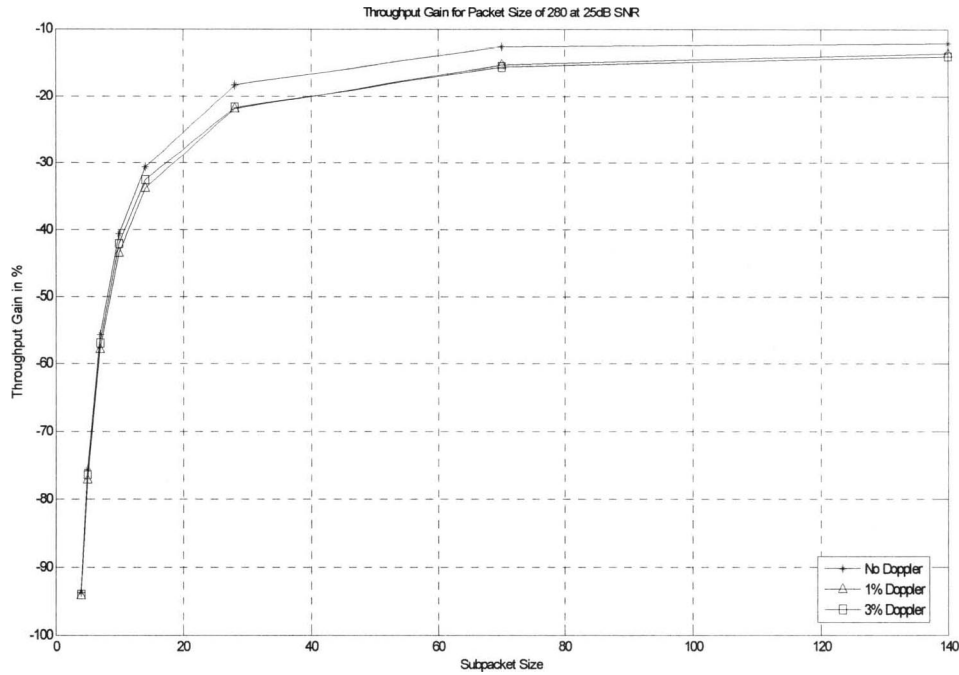


Figure 18. Throughput gain for packet length of 280 at 25dB

From Figure 18, Table 6 shows the throughput gain for a packet size of 280, at 25dB channel SNR without Doppler. With the identification overhead required for the proposed scheme, a packet size of 280 did not outperform the baseline scheme using the subpacket sizes studied.

Table 6. Throughput gain for packet length of 280 at 25dB without Doppler

Throughput Gain in %	Subpacket Size of 280 at 25dB SNR							
	4	5	7	10	14	28	70	140
Fade Rate 0%	-93.78	-75.51	-55.76	-40.56	-30.62	-18.38	-12.56	-12.21

For completeness, all other scenarios considered for the preparation of this project are documented in Appendix A.

## 2) Drop-Rate Comparison

Expressed in percentage, a positive drop-rate reduction is the improvement that the proposed scheme has over the baseline scheme with respect to the amount of dropped data because of reaching the maximum number of times for re-transmission. For instance, if the proposed scheme has a drop-rate of 60% while the baseline scheme is at 75%, the drop-rate reduction reported will be 20%. Figures 19 to 21 show the drop-rate reduction for packet lengths of 1400, 560 and 280 at a SNR of 25dB respectively.

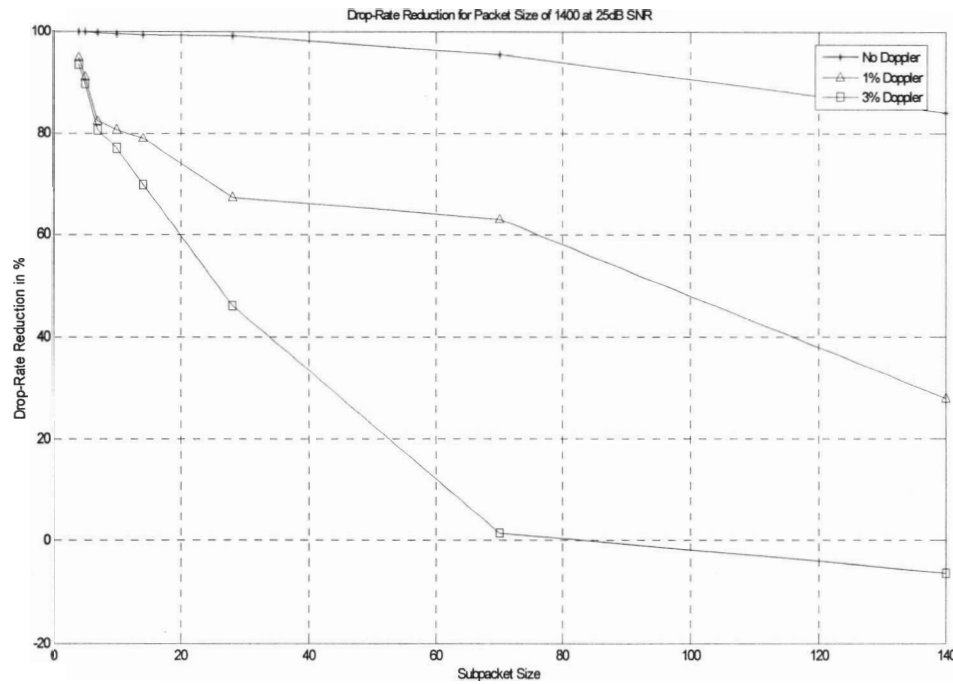


Figure 19. Drop-rate reduction for packet length of 1400 at 25dB

Figure 19 presents the drop-rate reductions for the packet size of 1400, at 25dB channel SNR with the fade rates studied. The results are tabulated in Table 7. At 25dB without Doppler, using the subpacket sizes of 10 or greater, the drop-rate reduction

ranges from 84% to 99%. Moreover, at Doppler of 1% with subpacket size of 70, the drop-rate reduction is over 60%.

Table 7. Drop-rate reduction for packet length of 1400 at 25dB with 0%, 1% and 3% Doppler

Drop-Rate Reduction in %		Subpacket Size of 1400 at 25dB SNR							
		4	5	7	10	14	28	70	140
Fade Rate	0%	99.98	99.93	99.71	99.57	99.32	98.94	95.51	84.04
	1%	94.87	91.05	82.39	80.69	78.96	67.22	62.90	27.73
	3%	93.59	89.64	80.57	76.96	69.76	46.01	1.56	-6.38

Figure 20 shows that for packet size of 560 25dB channel SNR with a fade rate of 0%, the drop-rate improvement is 74% when subpacket size of 70 is chosen.

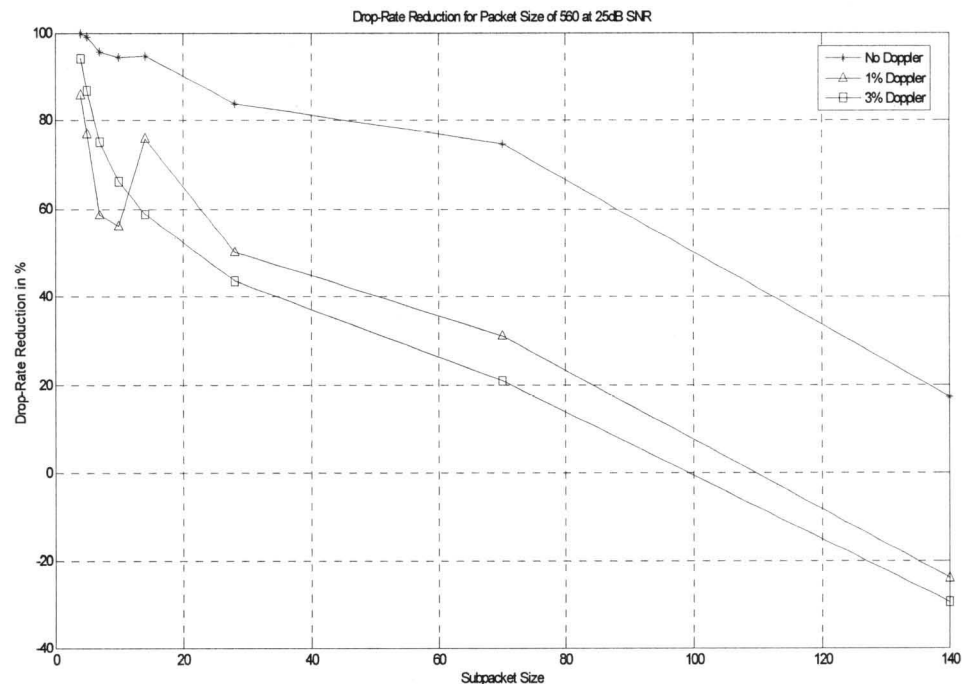


Figure 20. Drop-rate reduction for packet length of 560 at 25dB

Although other scenarios considered in this report also exhibit great improvement in drop-rate, the plots are presented in Appendix B and are excluded from this subsection because there are no throughput gains. Similar to the throughput analysis subsection, all other drop-rate results considered for the preparation of this project are documented in Appendix B.

### 3) Overall Performance Comparison

When a channel has a SNR of 25dB, employing the proposed scheme with selected subpacket sizes lead to a lower drop-rate and an improvement in throughput. A summary of notable results at 25dB presented in this subsection is in Table 8.

Table 8. Summary of the performance gain for the proposed scheme at 25dB SNR

Packet Size	Doppler	Subpacket Size	Throughput Gain	Drop-Rate Reduction
1400	0	28 and 70	35%	99% and 96%
	1%	28 and 70	1.6% and 6.7%	67% and 62%
560	0	70	0.3%	74%

Special attention should be paid to the results of scenarios without Doppler. Without Doppler, the throughputs of the proposed scheme using the subpacket sizes outlined in Table 8 are higher than or the same as the baseline scheme, with significant improvement in the drop-rate reductions as well. The results lead to the possibility of using of the proposed subpacket technique for deployment scenarios without fade rates.

## IV. FUTURE EXTENSIONS

There are several extensions to this investigation. One possible extension is to analytically determine the threshold values as a function of PSAM parameters, packet and subpacket sizes. Another extension is to use maximum ratio combining at the receiver to improve the overall system performance. A third extension is to incorporate the effects of co-channel interference and assess the feasibility of using this technique in other ARQ schemes, such as the various HARQ schemes in fixed mobile applications, for potential throughput improvement.

## V. CONCLUSIONS

A novel scheme of ARQ protocol using fixed-boundary subpackets to partition a packet for re-transmissions is presented. Monte Carlo simulations of transmitting PSAM signals using QPSK over Rayleigh channels without Doppler, as well as with 1% and 3% fade rates have been used to evaluate the performance of the proposed technique. Benchmarking against an ARQ protocol using CRC16-CCITT for error detection, this subpacket ARQ scheme provides up to 35% and 7% better in throughput for packets of 1400 when the channel SNR is greater than 25dB without Doppler and with 1% Doppler respectively. Moreover, lower drop-rates than the baseline scheme are found along with the throughput improvement reported in this project. Future extensions of this subpacket re-transmission scheme with PSAM may lead to higher throughput in other ARQ and HARQ protocols.

# APPENDICES

## Appendix A

Appendix A contains the throughput comparisons of all the scenarios considered for the preparation of this project.

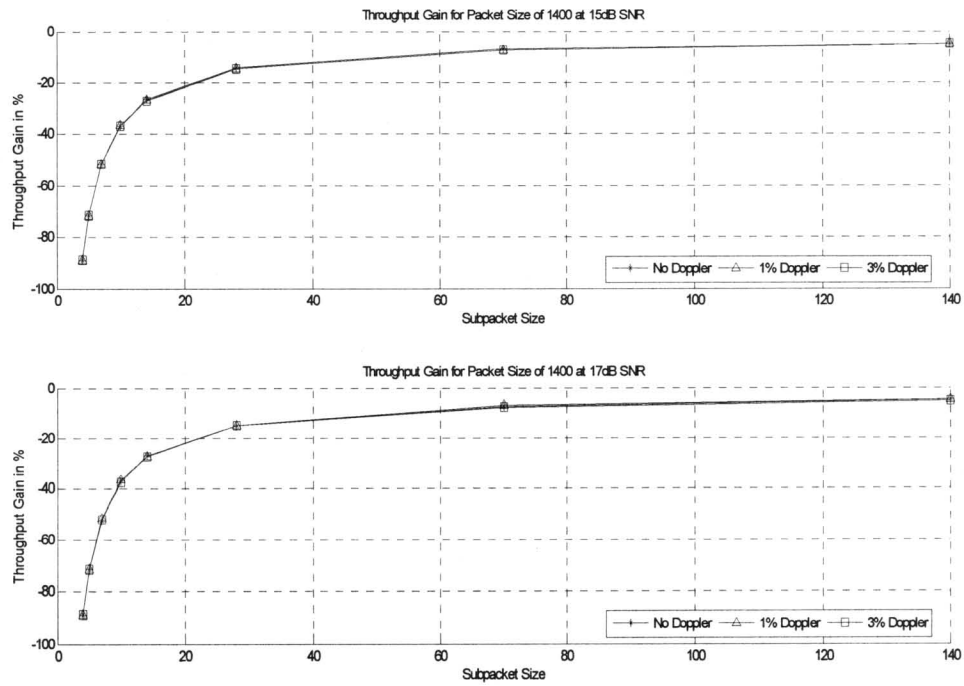


Figure 21. Throughput gain for packet length of 1400 at 15dB to 17dB



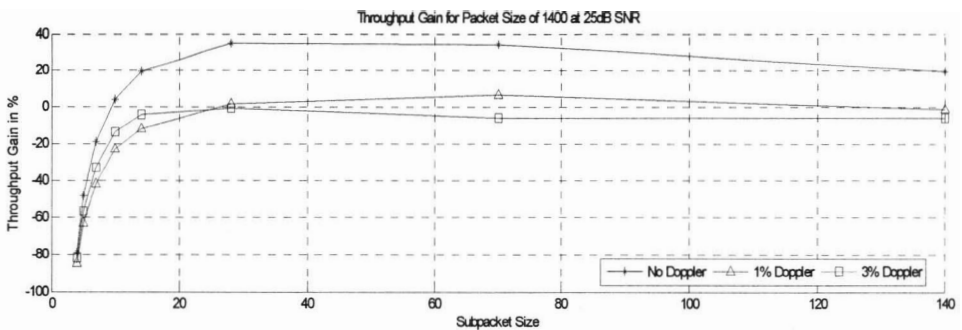
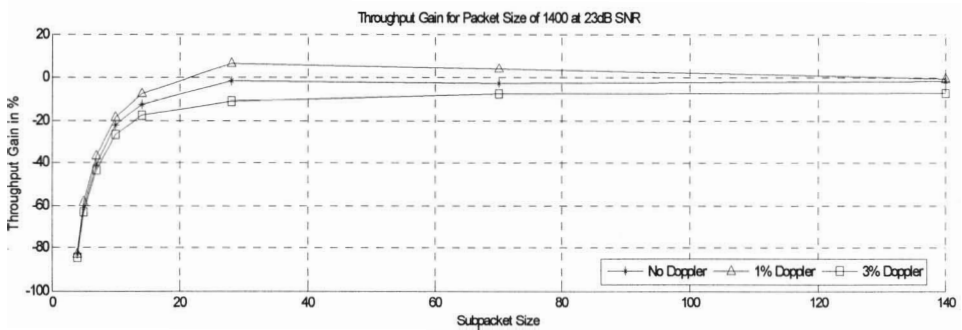
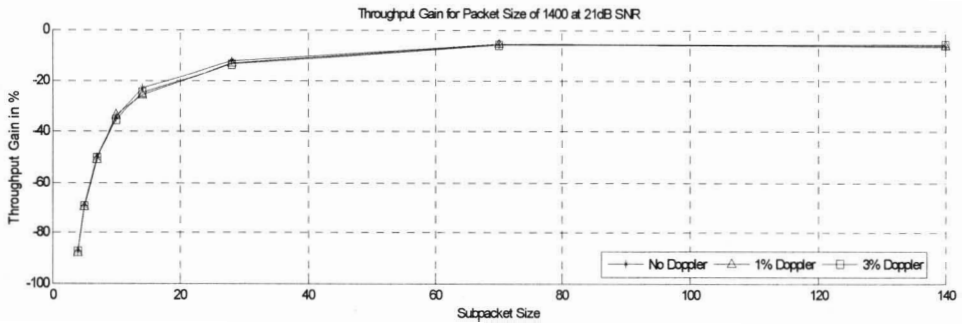
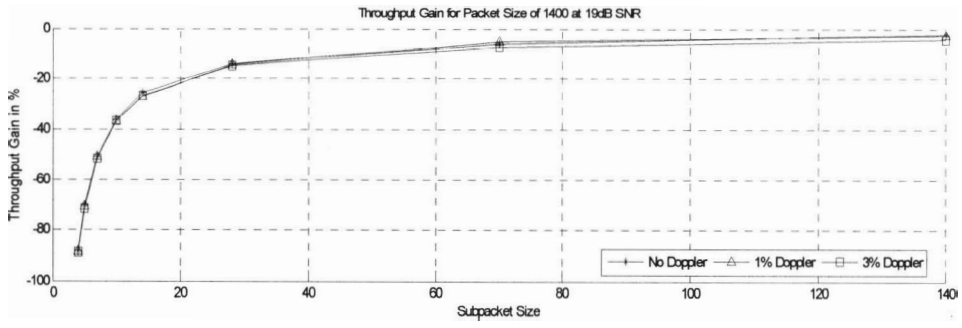


Figure 22. Throughput gain for packet length of 1400 at 19dB to 25dB

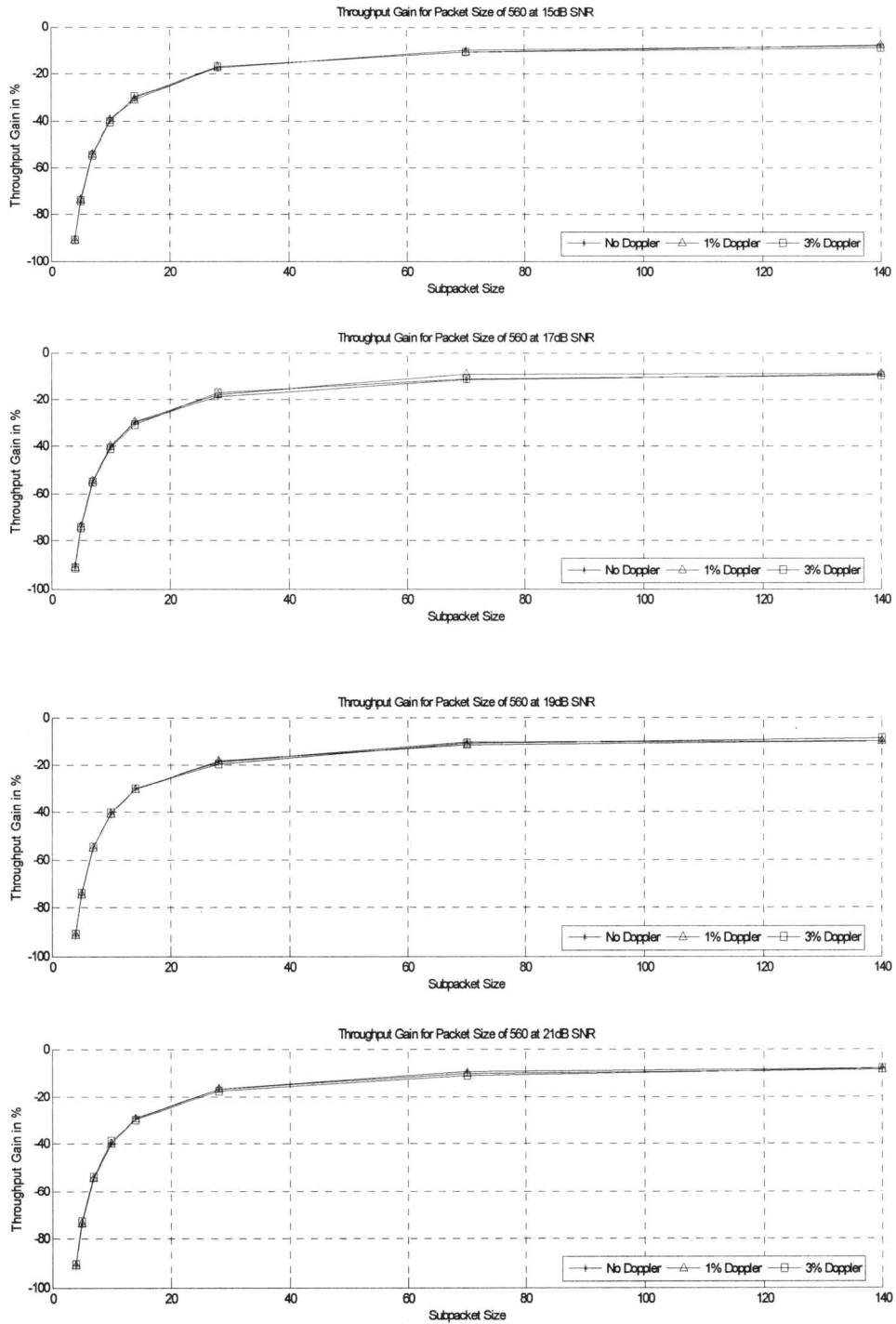


Figure 23. Throughput gain for packet length of 560 at 15dB to 21dB

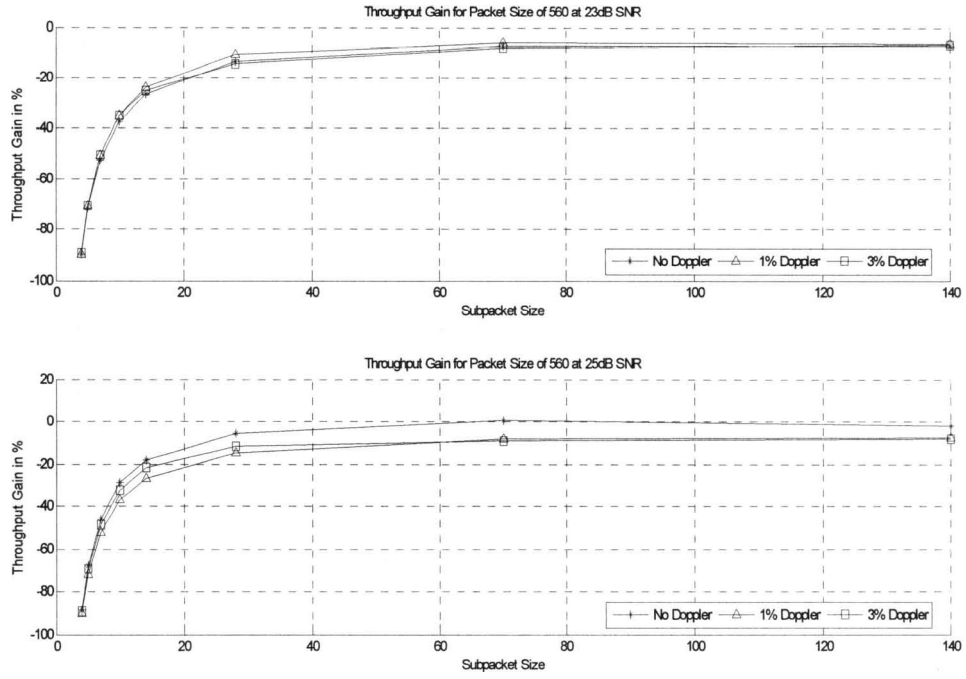


Figure 24. Throughput gain for packet length of 560 at 23dB to 25dB

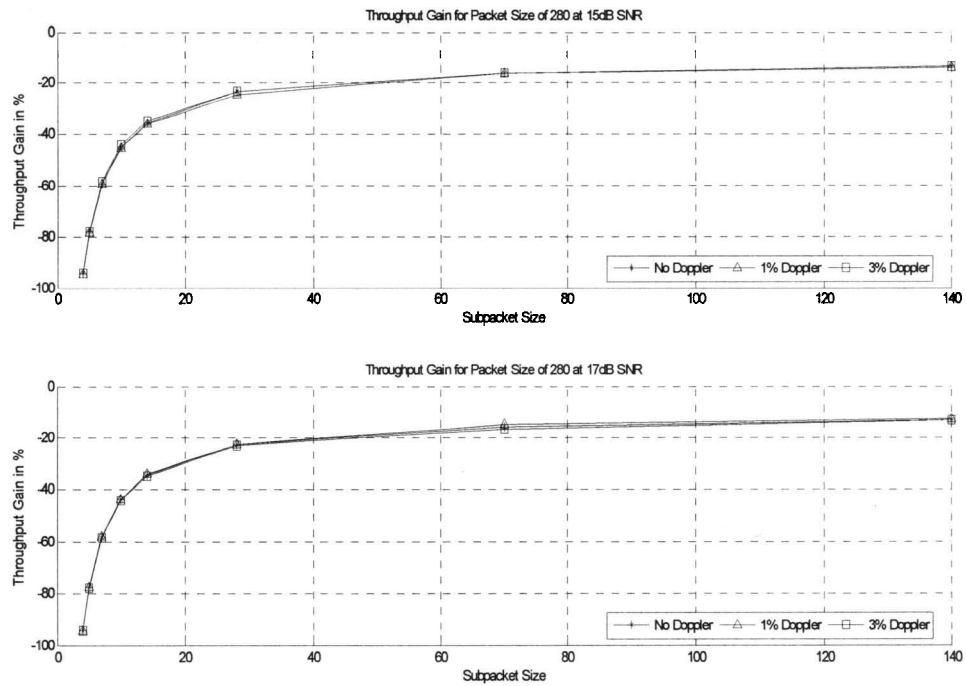


Figure 25. Throughput gain for packet length of 280 at 15dB to 17dB

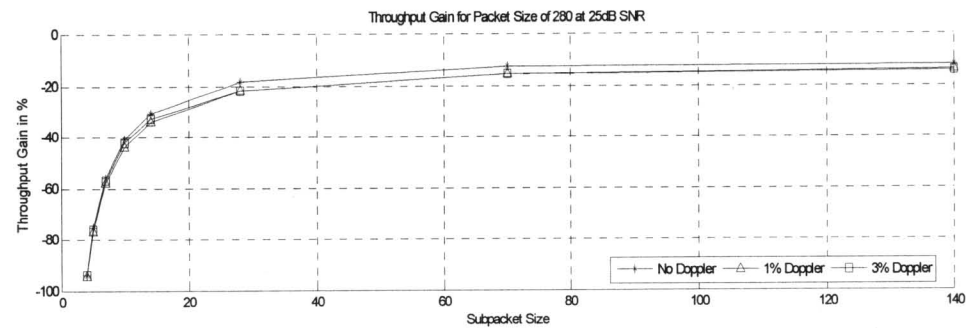
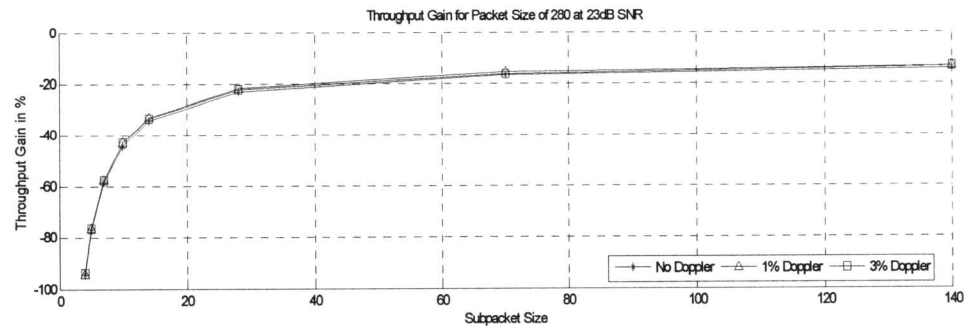
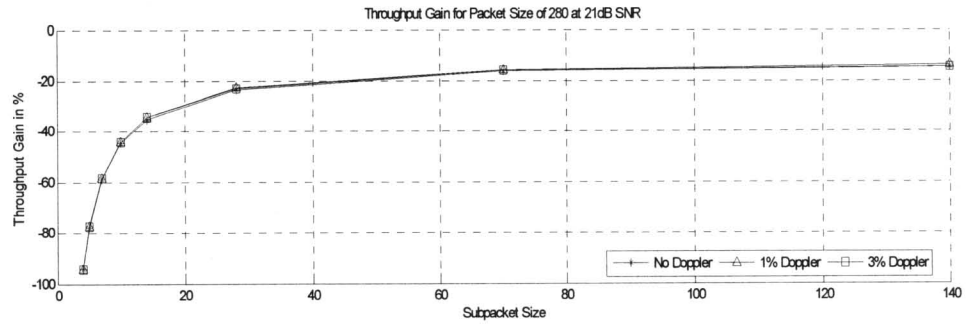
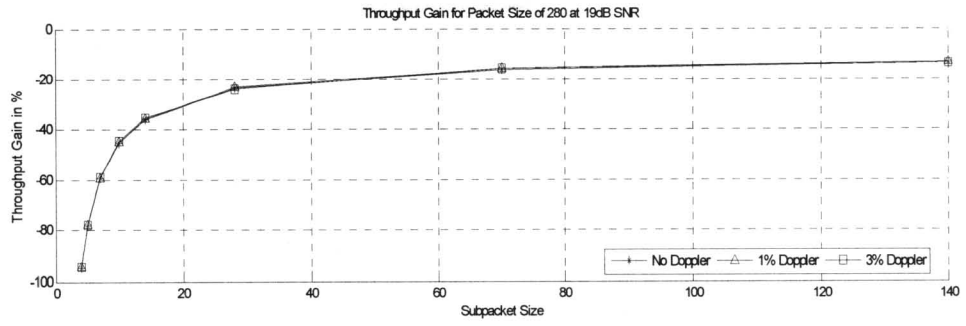


Figure 26. Throughput gain for packet length of 280 at 19dB to 25dB

## Appendix B

Appendix B contains the drop-rate of all the scenarios considered for the preparation of this project.

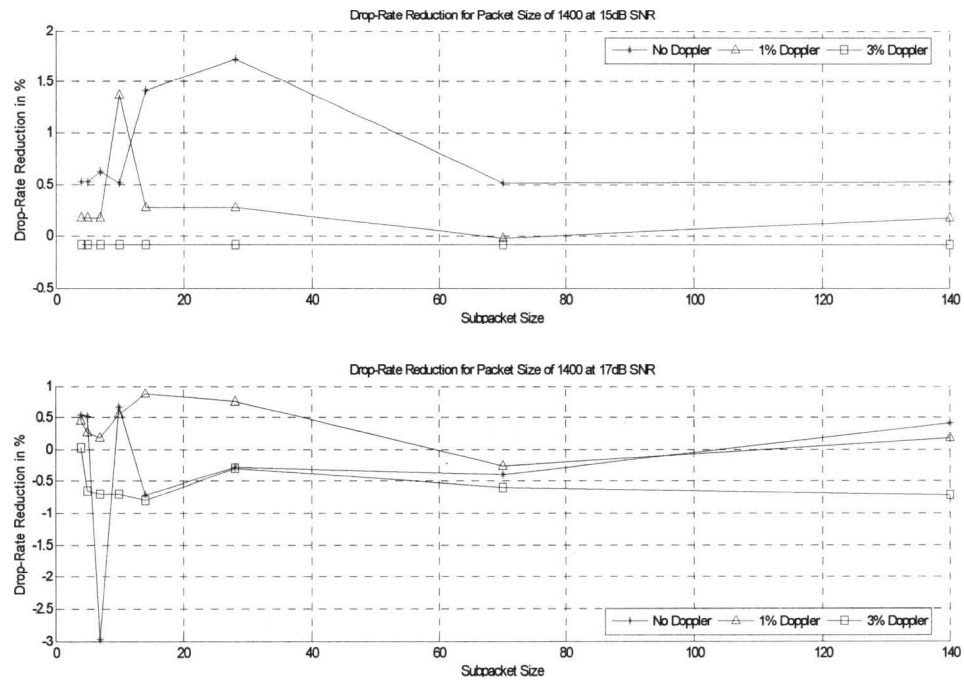


Figure 27. Drop-rate reduction for packet length of 1400 at 15dB to 17dB

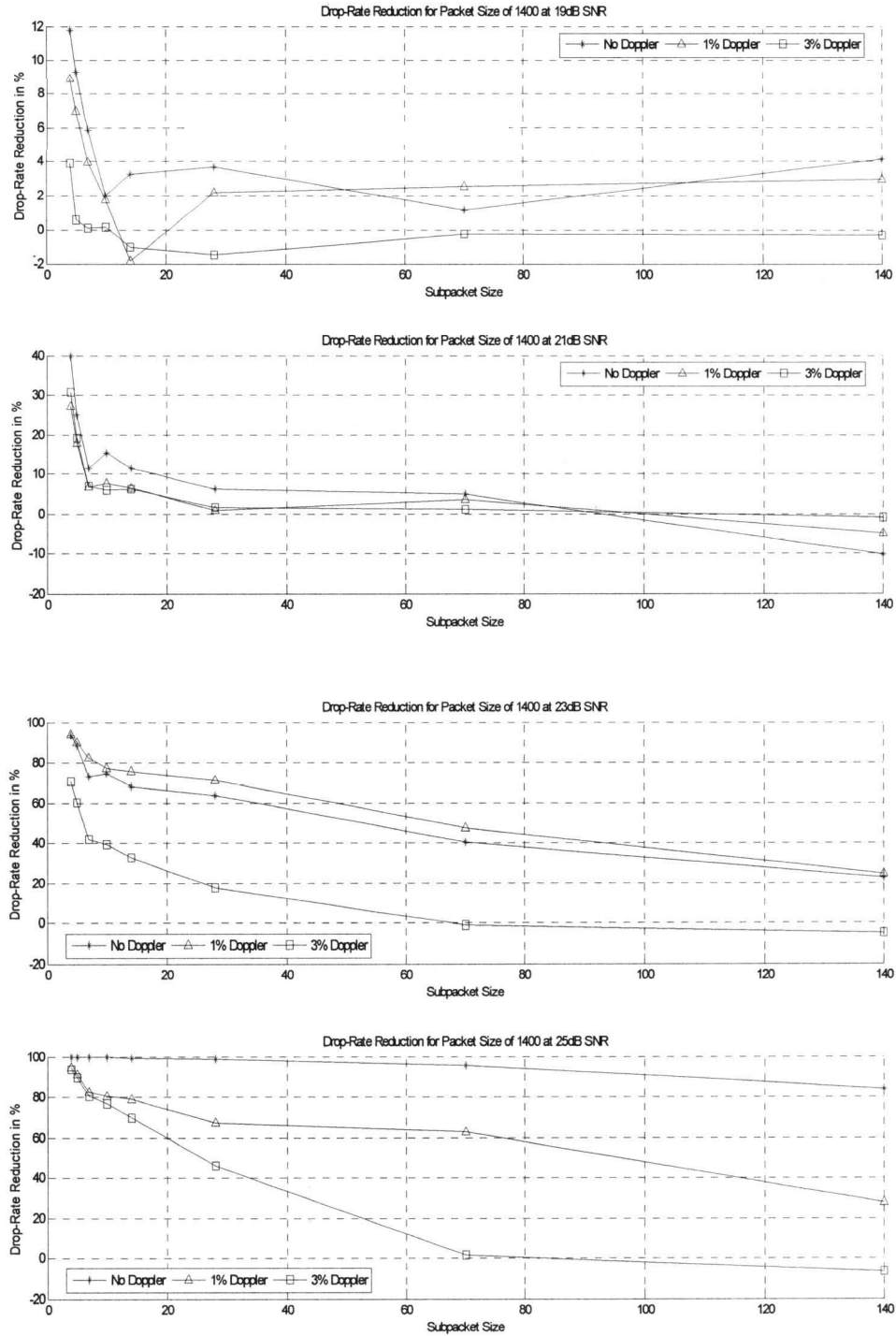


Figure 28. Drop-rate reduction for packet length of 1400 at 19dB to 25dB

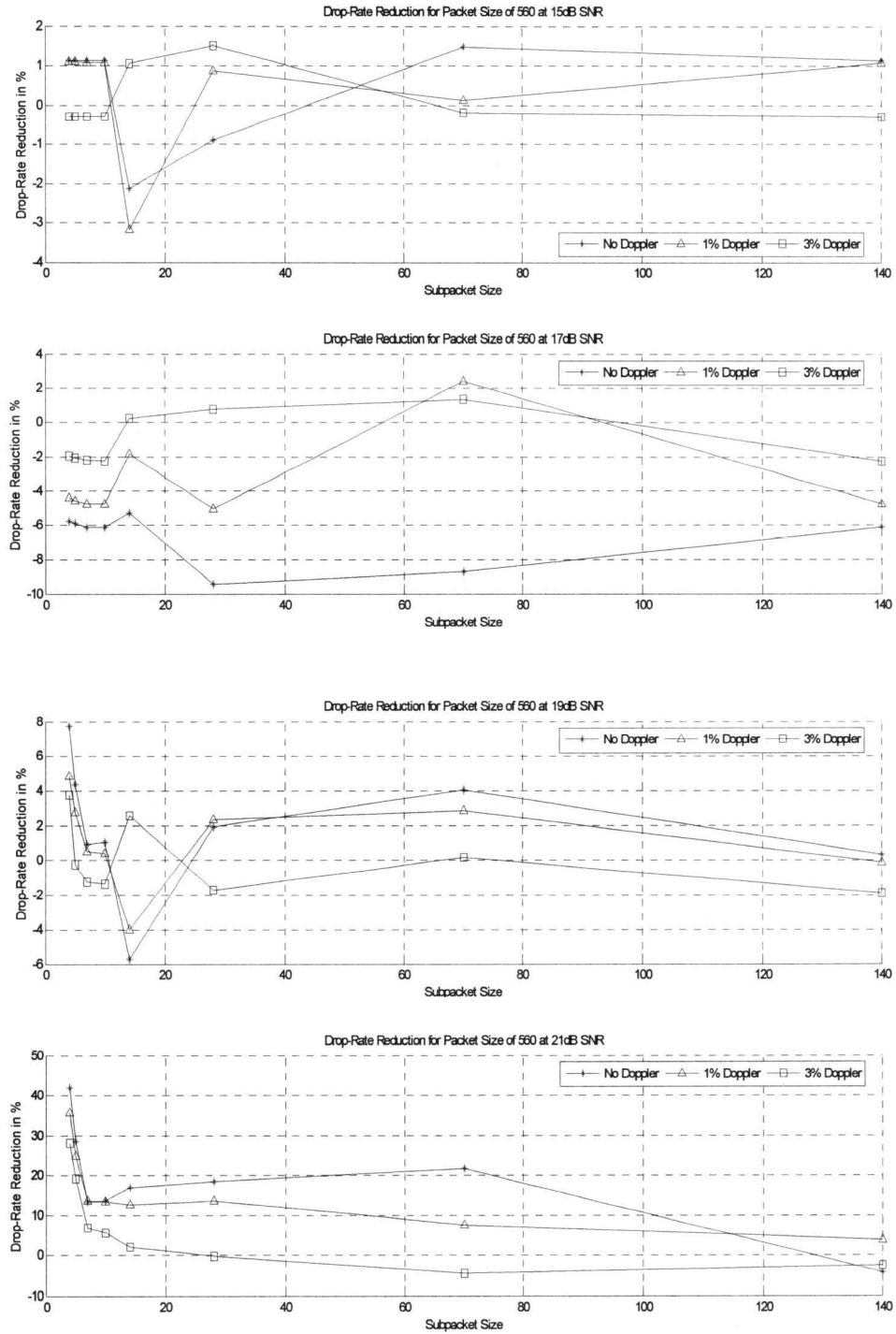


Figure 29. Drop-rate reduction for packet length of 560 at 15dB to 21dB

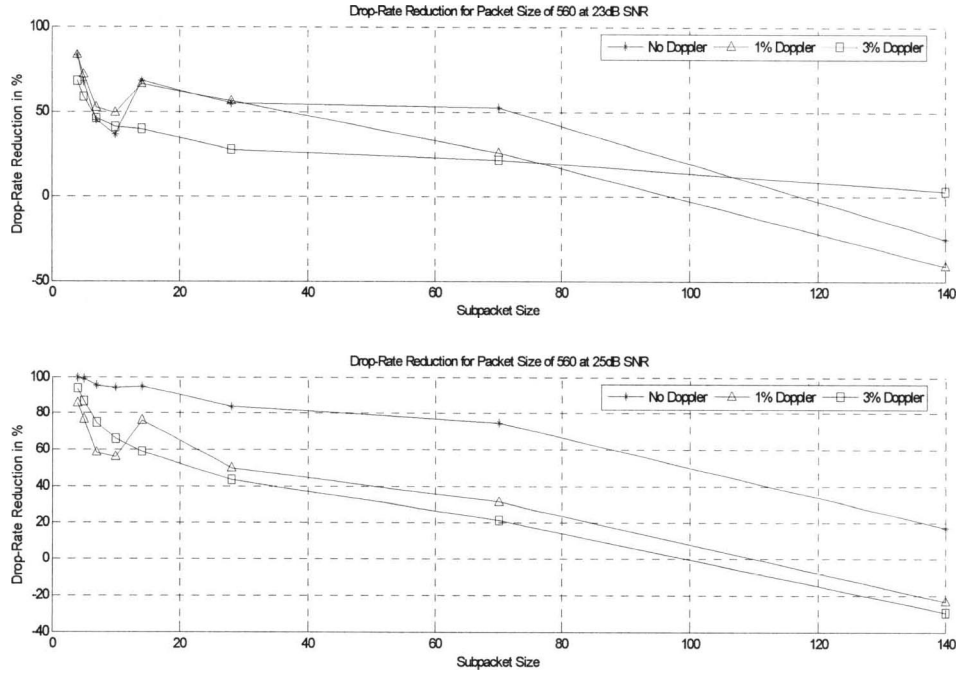


Figure 30. Drop-rate reduction for packet length of 560 at 23dB to 25dB

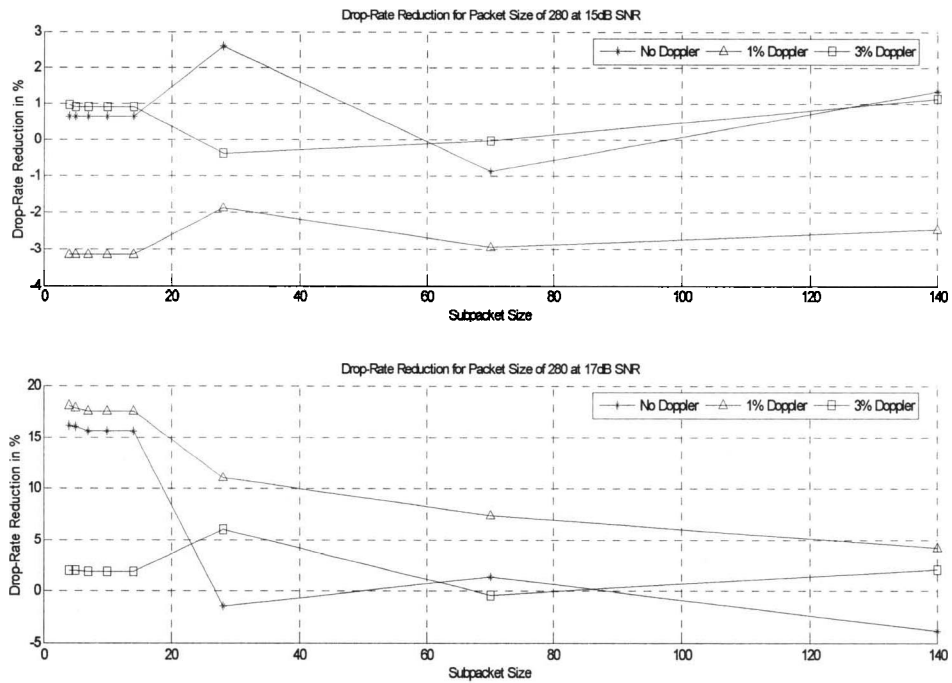


Figure 31. Drop-rate reduction for packet length of 280 at 15dB to 17dB



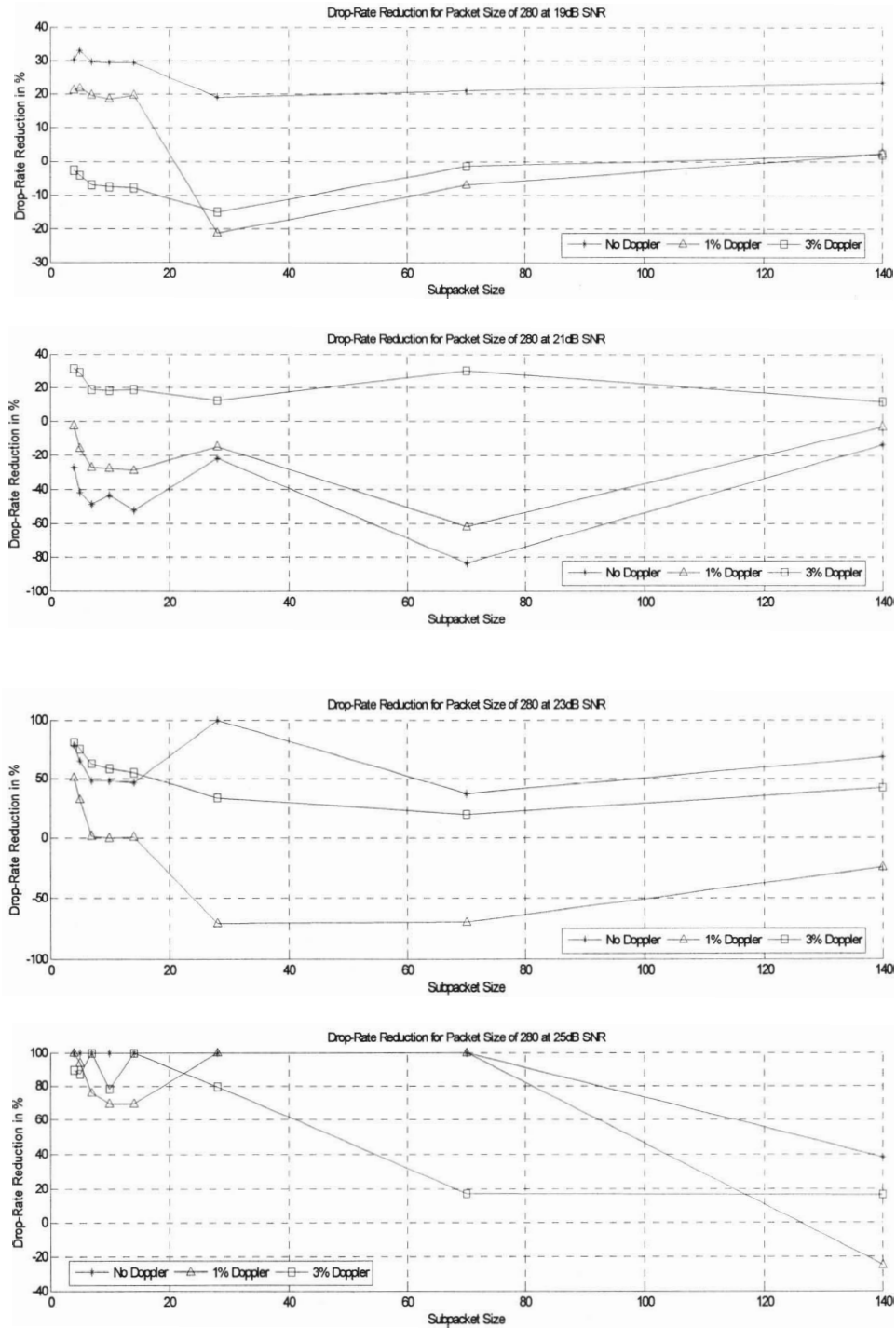


Figure 32. Drop-rate reduction for packet length of 280 at 19dB to 25dB

## REFERENCES

- [1] T. Ji and W. Stark, "Rate-Adaptive Transmission Over Correlated Fading Channels," *IEEE Transactions on Communications*, vol. 53, no. 10, pp. 1663-1670, Oct. 2005.
- [2] J. Chou and K. Ramchandran, "Arithmetic Coding-Based Continuous Error Detection for Efficient ARQ-Based Image Transmission," *IEEE Journal on Selected Areas in Communications*, vol. 18, no. 6, pp. 861-867, Jun. 2000.
- [3] J.-F. (T) Cheng, "Coding Performance of Hybrid ARQ Schemes," *IEEE Transactions on Communications*, vol. 54, no. 6, pp. 1017-1029, Jun. 2006.
- [4] E. Zimmermann, P. Herhold, G. Fettweis, "The Impact of Cooperation on Diversity-Exploiting Protocols," in *IEEE 59<sup>th</sup> Vehicular Technology Conference*, 17-19 May 2004, vol. 1, pp. 410-414.
- [5] G. Wade, *Coding Techniques: An Introduction to Compression and Error Control*. New York City, NY, USA: Palgrave, 2000, p. 198.
- [6] Y. Wang, L. Zhang, and D. Yang, "Performance Analysis of Type III HARQ with Turbo Codes," in *The 57<sup>th</sup> IEEE Semiannual Vehicular Technology Conference*, 22-25 Apr. 2003, vol. 4, pp. 2740-2744.
- [7] P. Frenger, S. Parkvall, and E. Dahlman, "Performance comparison of HARQ with Chase combining and incremental redundancy for HSDPA," in *IEEE VTS 54th Vehicular Technology Conference 2001*, 7-11 Oct. 2001, vol. 3, pp.1829-1833.
- [8] H. Zheng and H. Viswanathan, "Optimizing the ARQ Performance in Downlink Packet Data Systems With Scheduling," *IEEE Transactions on Wireless Communications*, vol. 4, no.2, March 2005.
- [9] K. Sawai and S. Uebayashi, "A Hybrid ARQ for Data Transmission in Digital Mobile Radio," in *IEEE 43<sup>rd</sup> Vehicular Technology Conference*, 18-20 May 1993, pp. 762-765.
- [10] S.S. Chakraborty, M. Liinajarja, and E. Yli-Juuti, "An Adaptive ARQ Scheme with Packet Combining for Time Varying Channels," *IEEE Communications Letters*, vol. 3, no. 2, pp.52-54, Feb. 1999.
- [11] E.C. Strinati, S. Simoens, and J. Boutros, "Performance evaluation of some Hybrid ARQ schemes in IEEE 802.11a Networks," in *The 57<sup>th</sup> IEEE Semiannual Vehicular Technology Conference*, 22-25 Apr. 2004, vol. 4, pp. 2735-2739.

- [12] B.A. Harvey, S.B. Wicker, "Packet Combining Systems Based on the Viterbi Decoder," *IEEE Transactions on Communications*, vol. 42, No. 2/3/4, pp. 1522-1557, Feb./Mar./Apr. 1994.
- [13] Y. Zhou and J. Wang, "Optimum Subpacket Transmission for Hybrid ARQ Systems," *IEEE Transactions on Communications*, vol. 54 no. 5, pp. 934-942, May 2006.
- [14] J.K. Cavers, "An Analysis of Pilot Symbol Assisted Modulation for Rayleigh Fading Channels," *IEEE Transactions on Vehicular Technology*, vol. 40, no. 4, pp. 686-693, Nov. 1991.
- [15] L. Welburn and J.K. Cavers, "Pilot Signals Improve the Performance of a Reed-Solomon Errors and Erasures Decoder in Rayleigh Fading Channels," *IEEE Transactions on Communications*, vol. 47, no. 5, pp. 689-696, May 1999.